# Engineering Science Data Booklet 

## Higher

For use in National Qualification Courses
leading to the 2015 examinations and beyond.

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## Preface

This data booklet is intended for use by candidates in examinations in Engineering Science at Higher. It may also be used as a reference for assignments at Higher. It is recommended that candidates should become familiar with the contents of the data booklet through use in undertaking Units of these Courses.

It should be noted that the range of data contained in the booklet has been limited to the concepts which may be assessed through written question papers. This range should be supplemented by other resource material as necessary during the course, eg by using data sheets. However, should any additional information (or data not included in this booklet) be required in an examination, such information will be included in the question paper.

Teachers/lecturers should note that all of the material contained in this booklet is likely to be examined at some time. With regard to tables of information, not every entry in a table will necessarily be involved in examination questions.

From the variety of data offered in this booklet, candidates will be expected to demonstrate the ability to select appropriate information or formulae.

Quantities, Symbols and Units

| Quantity | Symbol | Unit | Abbreviation |
| :---: | :---: | :---: | :---: |
| distance | d,x | metre | m |
| height | h | metre | m |
| length | 1 | metre | m |
| diameter | d | metre | m |
| radius | r | metre | m |
| area | A | square metre | $\mathrm{m}^{2}$ |
| circumference | C | metre | m |
| time | t | second | $s$ |
| speed, velocity | v | metre per second | $\mathrm{ms}^{-1}$ |
| mass | m | kilogram | kg |
| force | F | newton | N |
| gravitational acceleration | g | metre per second per second | $\mathrm{ms}^{-2}$ |
| work done | $\mathrm{E}_{\mathrm{w}}$ | joule | J |
| energy | E | joule | J |
| power | P | watt | W |
| torque | T | newton metre | Nm |
| efficiency | $\eta$ | - | - |
| pressure | P | newton per square metre (pascal) | $\mathrm{Nm}^{-2}(\mathrm{~Pa})$ |
| temperature | T | kelvin, celsius | K, ${ }^{\circ} \mathrm{C}$ |
| specific heat capacity | c | joule per kilogram per degree kelvin | $\mathrm{Jkg}^{-1} \mathrm{~K}^{-1}$ |
| voltage, potential difference | V | volt | V |
| current | I | ampere (amp) | A |
| resistance | R | ohm | $\Omega$ |
| frequency | f | hertz | Hz |
| rotational speed | n | revolutions per minute | revs $\mathrm{min}^{-1}$ |
|  |  | revolutions per second | revs sec ${ }^{-1}$ |
| stress | $\sigma$ | newton per square metre (pascal) | $\mathrm{Nm}^{-2}(\mathrm{~Pa})$ |
| strain | $\epsilon$ | - | - |

## Decimal Prefixes

| Prefix | Symbol | Multiplying factor |
| :--- | :---: | :---: |
| peta | P | $10^{15}$ |
| tera | T | $10^{12}$ |
| giga | G | $10^{9}$ |
| mega | M | $10^{6}$ |
| kilo | k | $10^{3}$ |
| milli | m | $10^{-3}$ |
| micro | $\mu$ | $10^{-6}$ |
| nano | n | $10^{-9}$ |
| pico | p | $10^{-12}$ |

## Relationships

## Energy and power

| Potential energy | $E_{p}=m g h$ | $\mathrm{g}=9.8 \mathrm{~ms}^{-2}$ (to 2 significant figures) |
| :---: | :---: | :---: |
| Kinetic energy | $E_{k}=1 / 2 m v^{2}$ |  |
| Heat energy | $E_{h}=c m \Delta T$ | $C_{\text {water }}=4200 \mathrm{Jkg}^{-1} \mathrm{~K}^{-1}$ (to 2 significant figures) |
| Electrical energy | $\mathrm{E}_{\mathrm{e}}=\mathrm{VII}$ |  |
| Work done | $\mathrm{E}_{\mathrm{w}}=\mathrm{Fd}$ |  |
| Power | $P=\frac{E}{t}$ |  |
| Electrical power | $\mathrm{P}=\mathrm{VI}=\frac{\mathrm{V}^{2}}{\mathrm{R}}=I^{2} \mathrm{R}$ |  |
| Mechanical power | $\mathrm{P}=\mathrm{Fv}$ | $P=2 \pi n T$ ( $n=$ no of revs per second) |
| Efficiency | $\eta=\frac{\text { Energy }_{\text {out }}}{\text { Energy }_{\text {in }}}=$ | $\frac{r_{\text {out }}}{e_{\text {in }}}$ |

## Mechanisms

Velocity ratio

Torque
Circumference of circle
Moment of force
Principle of moments

Conditions of equilibrium
$V R=\frac{\text { speed of input }}{\text { speed of output }}$
Input speed x input size $=$ output speed x output size
$\mathrm{T}=\mathrm{Fr}$
$C=\pi d$
$M=\mathrm{Fx} \quad$ ( x is perpendicular distance)
$\Sigma M=0$
$\Sigma$ clockwise moments $=\Sigma$ anti-clockwise moments
$\Sigma \mathrm{F}_{\mathrm{h}}=0$
$\Sigma F_{V}=0$
$\Sigma M=0$

## Pneumatic Systems

| Pressure, force and area | $P=\frac{F}{A}$ |
| :--- | :--- |
| Area of circle | $A=\pi r^{2} \quad A=\frac{\pi d^{2}}{4}$ |
|  | $\pi=3.14$ (to 3 significant figures) |

## Structures

Stress

$$
\sigma=\frac{F}{A}
$$

Strain $\epsilon=\frac{\Delta l}{l}$

Strain energy
$E_{s}=\frac{1}{2} F_{x}$

Young's Modulus

Factor of Safety
$E=\frac{\sigma}{\epsilon}$
$=\frac{\text { ultimate load }}{\text { safe working load }}=\frac{\text { ultimate stress }}{\text { safe working stress }}$

Properties of materials

| Material | Young's <br> Modulus <br> $\mathbf{E}$ <br> kNm | Yield <br> stress <br> $\sigma_{\gamma}$ <br> $\mathbf{N m m}^{-2}$ | Ultimate <br> tensile <br> stress <br> $\mathbf{N m m}^{-2}$ | Ultimate <br> compressive <br> stress <br> $\mathbf{N m m}^{-2}$ |
| :--- | :---: | :---: | :---: | :---: |
| Mild steel | 196 | 220 | 430 | 430 |
| Stainless steels | $190-200$ | $286-500$ | $760-1280$ | $460-540$ |
| Low-alloy steels | $200-207$ | $500-1980$ | $680-2400$ | $680-2400$ |
| Cast iron | 120 | - | $120-160$ | $600-900$ |
| Aluminium alloy | 70 | 250 | 300 | 300 |
| Titanium alloy | 110 | 950 | 1000 | 1000 |
| Nickel alloys | $130-234$ | $200-1600$ | $400-2000$ | $400-2000$ |
| Concrete | - | - | - | 60 |
| Concrete (steel reinforced) | $45-50$ | - | - | 100 |
| Concrete (post stressed) | - | - | - | 100 |
| Plastic, ABS polycarbonate | $2 \cdot 6$ | 55 | 60 | 85 |
| Plastic, polypropylene | $0 \cdot 9$ | $19-36$ | $33-36$ | 70 |
| Wood, parallel to grain | $9-16$ | - | $55-100$ | $6-16$ |
| Wood, perpendicular to grain | $0 \cdot 6-1 \cdot 0$ | - | - | $2-6$ |

Electrical and electronic

Ohm's Law

Resistors in series

Resistors in parallel

2 resistors in parallel

Kirchhoff's 1st law

Kirchhoff's 2nd law

Voltage Divider

Electrical power
$V=I R$
$R_{t}=R_{1}+R_{2}+R_{3}+\ldots .$.
$\frac{1}{R_{t}}=\frac{1}{R_{1}}+\frac{1}{R_{2}}+\frac{1}{R_{3}}+\ldots$.
$R_{t}=\frac{R_{1} R_{2}}{\left(R_{1}+R_{2}\right)}$
$\Sigma \mathrm{I}=0$ (algebraic sum of currents at a node is zero)
$\Sigma \mathrm{E}=\Sigma \mathrm{I} \mathrm{R}$
(algebraic sum of supply voltages = sum of voltage-drops, in a closed loop)
$\frac{V_{1}}{V_{2}}=\frac{R_{1}}{R_{2}}$
$\mathrm{P}=\mathrm{VI}=\frac{\mathrm{V}^{2}}{\mathrm{R}}=I^{2} \mathrm{R}$

## Transistors

Bi-polar transistor gain
$h_{\text {FE }}=I_{c} / I_{b}$
MOSFET transconductance

MOSFET Characteristics Curves


## Typical operational amplifier circuits

$\mathrm{V}_{\mathrm{o}}=$ output voltage
$\mathrm{V}_{\mathrm{i}}=$ input voltage
$\mathrm{V}_{\mathrm{cc}}=$ supply voltage
$R_{f}=$ feedback resistance
$\mathrm{R}_{\mathrm{i}}=$ input resistance
$A_{v}=$ gain $=\frac{\text { output voltage }}{\text { input voltage }}$

Note : Op-amp output saturates at $85 \%$ of $\mathrm{V}_{\text {cc }}$

Inverting

$A_{v}=\frac{V_{0}}{V_{i}}$
$A_{v}=-\frac{R_{f}}{R_{i}}$
$V_{o}=-\frac{R_{f}}{R_{i}} V_{i}$

Non-inverting


$$
A_{v}=\frac{V_{0}}{V_{i}} \quad A_{v}=1+\frac{R_{f}}{R_{i}} \quad V_{o}=\left(1+\frac{R_{f}}{R_{i}}\right) V_{i}
$$

## Comparator



If $\mathrm{V}_{\mathrm{i}}<\mathrm{V}_{\text {ref }}$, then $\mathrm{V}_{0}$ saturates positively ( $85 \%$ of $+\mathrm{V}_{\text {cc }}$ )
If $\mathrm{V}_{\mathrm{i}}>\mathrm{V}_{\text {ref }}$, then $\mathrm{V}_{0}$ saturates negatively ( $85 \%$ of $-\mathrm{V}_{\mathrm{cc}}$ )

Difference Amplifier

$A_{v}=\frac{V_{0}}{\left(V_{2}-V_{1}\right)}$
$A_{v}=\frac{R_{f}}{R_{i}}$
$V_{0}=\frac{R_{f}}{R_{i}}\left(V_{2}-V_{1}\right)$

Summing Amplifier


$$
\begin{aligned}
& A_{v 1}=-\frac{R_{f}}{R_{1}} \quad A_{v 2}=-\frac{R_{f}}{R_{2}} \quad A_{v n}=-\frac{R_{f}}{R_{n}} \\
& V_{o}=\left(A_{v 1} V_{1}\right)+\left(A_{v 2} V_{2}\right)+\ldots \\
& V_{o}=-R_{f}\left(\frac{V_{1}}{R_{1}}+\frac{V_{2}}{R_{2}}+\ldots\right)
\end{aligned}
$$

Voltage Follower

[END OF DATA BOOKLET]

